



# Coping with the Collapse: A Stock-Flow Consistent, Monetary Macro-dynamics of Global Warming

June 23, 2016

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*développeur d'avenirs durables*

# ■ Outlines

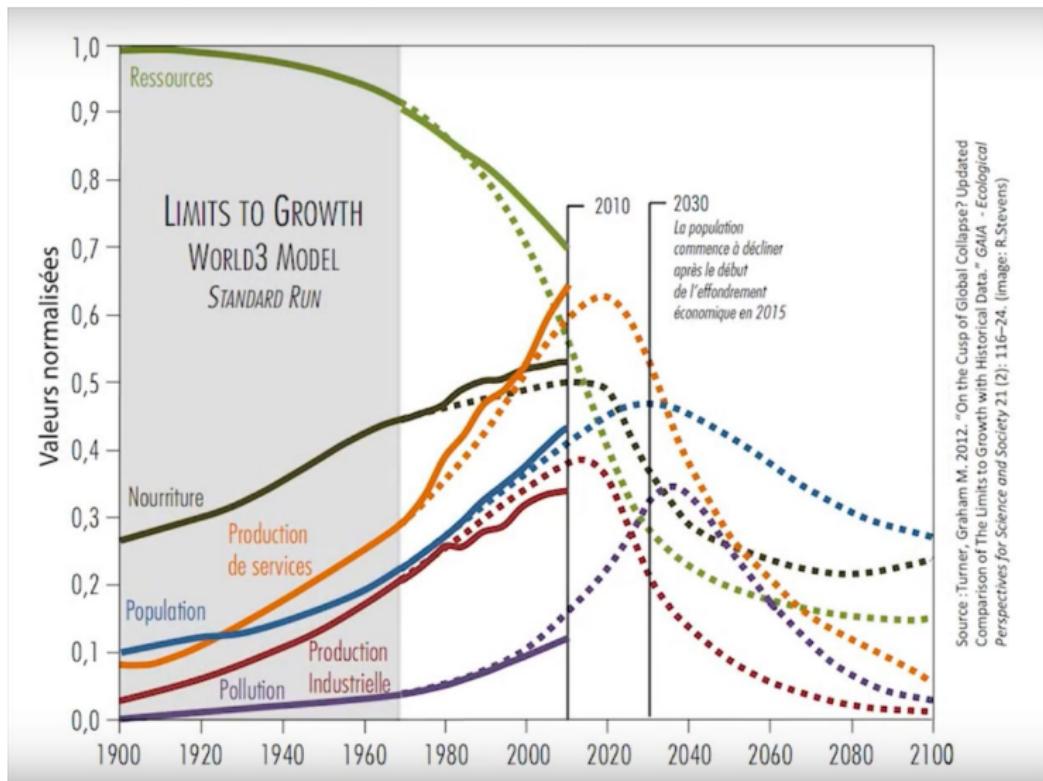
- 1 Introduction
- 2 The Keen (1995) Model
- 3 Macroeconomic model for climate change
- 4 Climate Module
- 5 Public Policy Module
- 6 Numerical Simulations
- 7 Further Work

## ■ Introduction

- *The Limits to Growth* was published (Meadows et al., 1972 and Meadows et al., 1974).
- Turner (2008, 2012, 2014) and Hall and Day (2009) tend to confirm the LtG standard run scenarios.

# ■ Introduction

*Sustainable path or collapse?*



## ■ Introduction

- Consistent with increasing capital costs and net energy (the decline of energy returned on energy invested, EROI).
- Growing scarcity of natural resources (energy, minerals, water...), while climate change plays little role, if any. (Caveat: Pollution).
- The question of whether global warming might *per se* induce a similar breakdown of the world economy (cf. COP 21).

## ■ Introduction

### *Paper's framework*

- We explicitly model the financial side of the world economy in order to assess the possible negative feedback of debt on the ability of the world economy to cope with the collapse.
- Pivotal role of private debt.
- Losses due to environmental damages force the global productive sector to invest a growing part of its wealth in restoring and maintaining capital.
- The persistent level of debt may endanger the world economic engine itself as it is based on the promise of future wealth creation.

## ■ Introduction

### *Paper's framework*

- Depending upon the speed at which labor productivity increases compared to the severity of global warming, the shrink of investment induced by the burden of private debt may prevent the world economy from further adapting to the climate turmoil, leading ultimately to a collapse around the end of the twenty-first century.
- The global collapse captured in this paper can be interpreted as the result of a debt-deflation depression in the sense given to this concept by Irving Fisher (1933).
- That part of the world economy might be on the verge of falling into a liquidity trap is illustrated, today, by the two “lost decades” of Japan, of course, but also the recessionary state of the Southern part of the Eurozone, obstinately negative long-term interest rates on international financial markets and, last but not least, the brutal contraction of the world nominal GDP in 2015 (-6%, IMF (2016)).

## ■ Introduction

*Paper's framework*

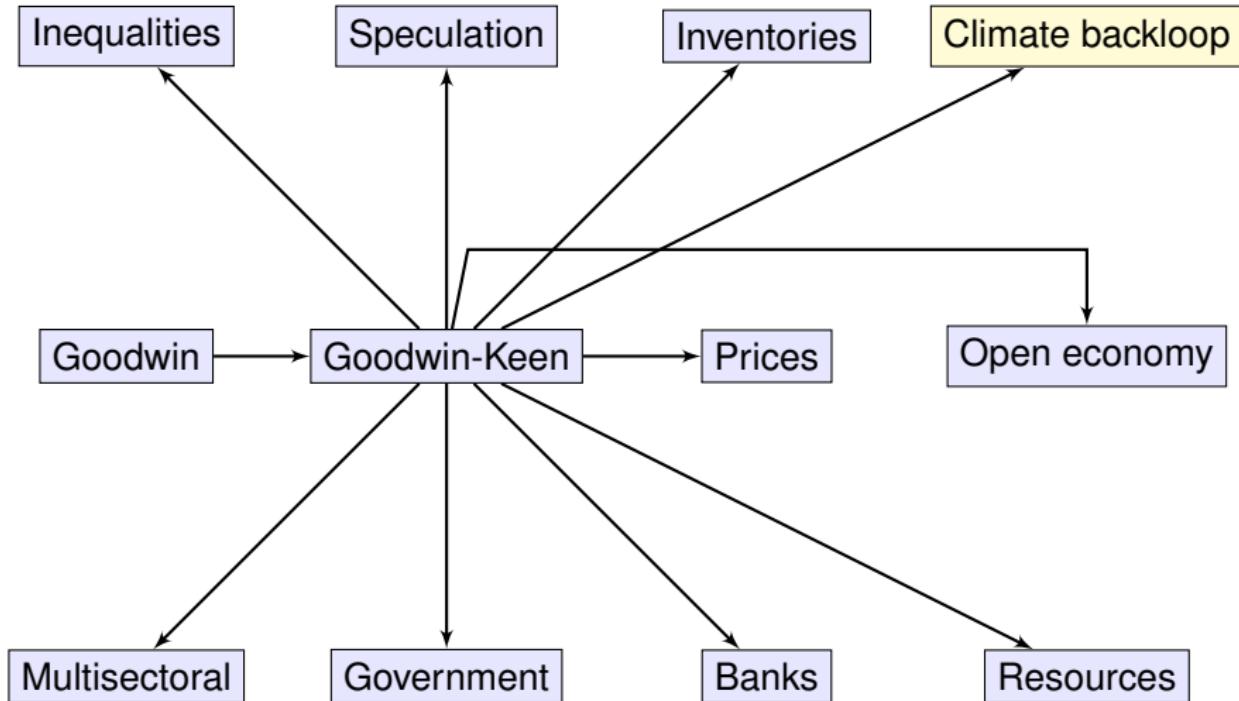
- These paradoxes may be viewed as signals of the translation of a secular decline induced by biophysical constraints into the financial sphere.

# ■ GEMMES

GEMMES

GEneral Monetary Multisectoral Macrodynamics for the Ecological Shifts

# GEMMES



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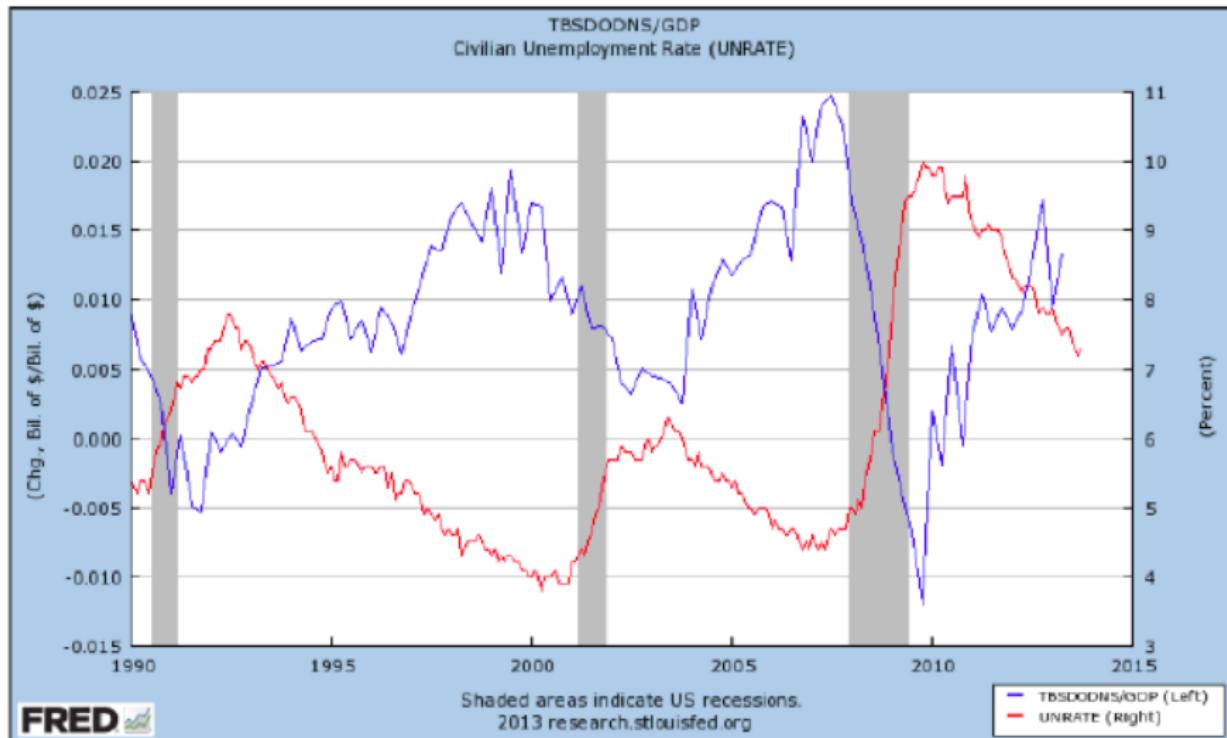
## ■ The Keen (1995) Model

### *Overview*

1. Since the financial crisis of 2007-2009, the ideas of Hyman Minsky around the intrinsic instability of a monetary market economy have experienced a significant revival.
2. Goodwin (1967): Lotka-Volterra logic of the wage share and the employment rate.
3. Keen (1995): 'Black Swan' event, or a Minsky moment can occur.
4. Investment financed by endogenous money creation.

# The Keen (1995) Model

*Private debt matters*



# The Keen (1995) Model

*Stock and Flow consistent model*

Balance Sheet	Households	Firms	Banks	Government	Sum
Capital stock		$K$			$K$
Loan		$-D$		$D$	
Sum (net worth)		$X^f$	$X^b$		$X$
Transactions		current	capital		
Consumption	$-C$	$C$			
Investment		$I$	$-I$		
Government spend.		$G$		$-G$	
Memo [GDP]		$[GDP]$			
Wages	$W$	$-W$			
Interests on debt		$-rD$		$rD$	
Firms' net profit		$-\Pi$	$\Pi$		
Financial Balances			$-\dot{D}$	$\Pi^b$	
Flow of funds					
Investment		$I$			$I$
Change in Loans		$-\dot{D}$	$\dot{D}$		
Column sum		$\Pi$	$\dot{D}$		$I$
Change in Net worth		$\dot{X}^f = \Pi + (\dot{p} - \delta p)K$	$\dot{X}^b = \Pi^b$		$\dot{X}$

Table: Stock-Flow Table

## ■ The Keen (1995) Model

*The model*

$\lambda$ : the employment rate.

$$\lambda := \frac{L}{N}.$$

$L$ : the labor force, and  $N$ : the total population.

$$\frac{\dot{N}}{N} = \beta.$$

$a$ : the labor productivity.

$$\frac{\dot{a}}{a} = \alpha.$$

$w$ : the wage per worker,  $W = wL$ : the total wage,  $\omega$ : the wage share  
and  $Y$ : the production.

$$\omega = \frac{W}{Y} = \frac{wL}{aL} = \frac{w}{a}$$

## ■ The Keen (1995) Model

*The model*

$K$ : the stock of capital.

$$\dot{K} = I - \delta K.$$

The Leontief production function

$$\begin{aligned} Y &= \min \left( \frac{K}{\nu}, aL \right) \\ &= \frac{K}{\nu} = aL. \end{aligned}$$

## ■ The Keen (1995) Model

*The model*

$D$ : the aggregate debt.

$$\dot{D} = I - \Pi.$$

with  $\Pi := Y - W - rD$ : the real profit of the firm, and  $r$ : the interest rate.

$\pi$ : the profit-to-production ratio.

$$\pi = \frac{\Pi}{Y}.$$

$d$ : the debt-production ratio.

$$d = \frac{D}{Y}.$$

## ■ The Keen (1995) Model

*Aggregate behaviours*

- The Short-term Phillips Curve (Mankiw, 2010).

$$\frac{\dot{w}}{w} = \phi(\lambda).$$

- The Investment Function : it evolves positively with the profit share.

$$\frac{I}{Y} = \kappa(\pi).$$

## ■ The Keen (1995) Model

*The three-dimensional system*

One can retrieve the following set of equations:

$$\dot{\omega} = \omega [\phi(\lambda) - \alpha]$$

$$\dot{\lambda} = \lambda \left[ \frac{\kappa(\pi)}{\nu} - \delta - \alpha - \beta \right]$$

$$\dot{d} = d \left[ r - \frac{\kappa(\pi)}{\nu} + \delta \right] + \kappa(\pi) - (1 - \omega)$$

## ■ The Keen (1995) Model

*Aggregate behaviours*

- Phenomenological approach:  $\phi(\cdot)$  and  $\kappa(\cdot)$  are empirically estimated.
- Sonnenschein-Mantel-Debreu (1975): anything can happen.
- Agent-based model.

## ■ The Keen (1995) Model

*Equilibria analysis*

Three long run equilibria exist:

- An unstable equilibrium at  $(0, 0, d_0)$
- A **good** equilibrium locally stable
- A **bad** equilibrium locally stable

## ■ Simulations - good equilibrium with finite debt

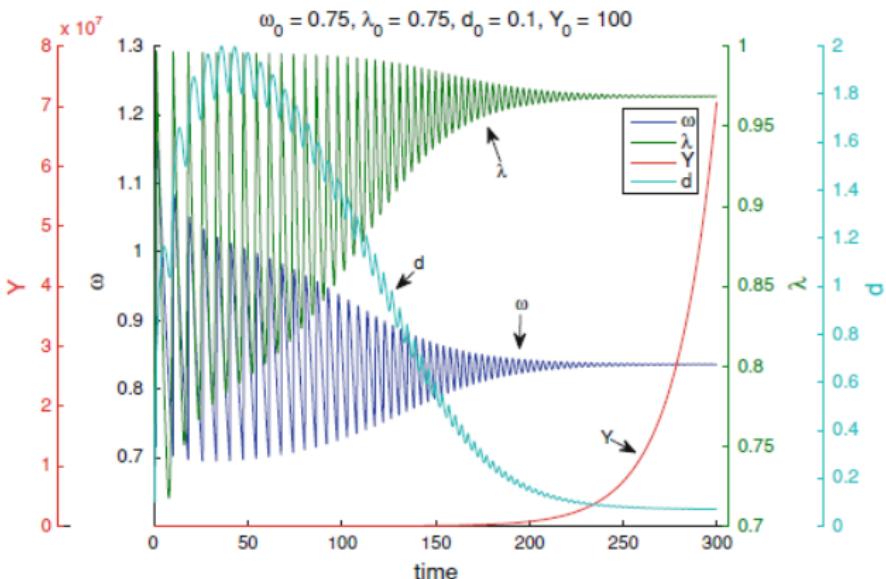


Fig. 4 Employment, wages, debt and output as functions of time converging to a stable equilibrium with finite debt in the Keen model

## ■ Simulations - bad equilibrium with infinite debt

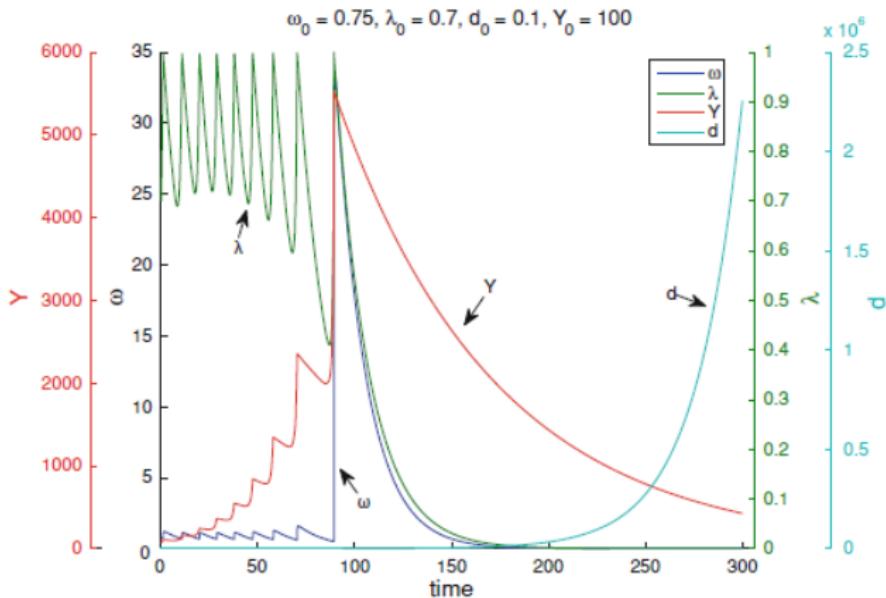
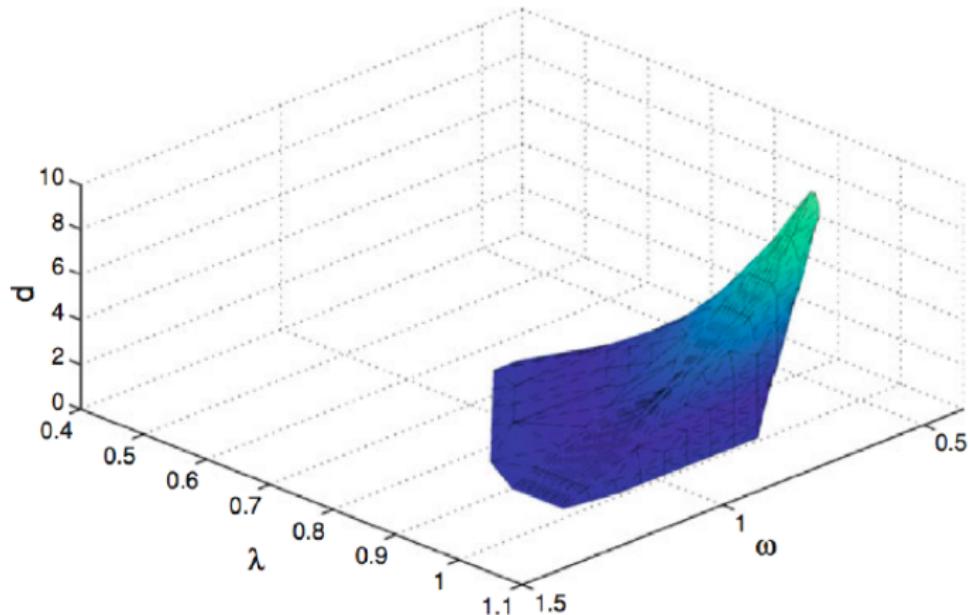


Fig. 5 Employment, wages, debt and output as functions of time converging to a stable equilibrium with infinite debt in the Keen model

## ■ Basin of Attraction



## ■ The Keen (1995) Model

*Possible outcome induced by climate change*

- Depending upon the basin of attraction where the state of the economy is driven by climate damages, the ultimate breakdown may occur as the inescapable consequence of the business as usual trajectory.

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## ■ Macroeconomic model for climate change

- Modelling:
  - The macroeconomics is borrowed from Keen (1995).
    - Stock-Flow consistent.
    - Phenomenological functions.
  - The climate feed-back loop is in line with Nordhaus' DICE model (2013).
- Estimation
  - Calibration of the climate and public policy modules in line with Norhdaus' DICE model (2013).
  - Macroeconomic module estimation in progress: panel analysis to benefit wider volatility.

## ■ Macroeconomic model for climate change

*Production, capital and debt accumulation*

The real output

$$Y = (1 - \mathbf{D}) \frac{K}{\nu}.$$

The investment function with abatement cost

$$I = (\kappa(\pi) - \mu G) Y.$$

Population grows according to a UN scenario,

$$\frac{\dot{N}}{N} = q(1 - \frac{N}{M}).$$

## ■ Macroeconomic model for climate change

*Monetary economy*

The wage dynamic evolves according to a short-term Phillips curve

$$\frac{\dot{w}}{w} = \Phi(\lambda) + \gamma i.$$

The price dynamics,

$$\begin{aligned} i &= \frac{\dot{p}}{p}, \\ &= \eta_p(m\omega - 1) + i_{LT}. \end{aligned}$$

## ■ Macroeconomic model for climate change

*Impact of climate change*

As an example, for deterministic exponential scenario, climate change positively impact the share of wages

$$\begin{aligned}\frac{\dot{\omega}}{\omega} &= \frac{\dot{w}}{w} - \frac{\dot{a}}{a} + \frac{\dot{\mathbf{D}}}{1-\mathbf{D}} - i \\ &= \phi(\lambda) - \alpha + \frac{\dot{\mathbf{D}}}{1-\mathbf{D}} - (1-\gamma)i.\end{aligned}$$

# ■ Macroeconomic model for climate change

	Households	Firms	Banks	Sum
<b>Balance Sheet</b>				
Capital stock		$+p_t K_t$		$+p_t K_t$
Loan		$-D_t$	$+D_t$	
Sum (net worth)		$X_t^f$	$X_t^b$	$X_t$
<b>Transactions</b>				
Consumption	$-p_t C_t$	current	capital	
Investment		$+p_t C_t$		
		$+p_t I_t$	$-p_t I_t$	
Accounting memo [GDP]		$[p_t Y_t (1 - \Delta_t)]$		
Wages	$+W_t$	$-W_t$		
Interests on debt		$-r D_t$		$+r D_t$
Firms' net profit		$-\Pi_t$	$+\Pi_t$	
Dividends	$+D_t$		$-D_t$	
Financial Balances			$-\dot{D}_t$	$+\Pi_t^b$
<b>Flow of funds</b>				
GFCF		$+p_t I_t$		$+p_t I_t$
Change in Loans		$-\dot{D}_t$	$+\dot{D}_t$	
Column sum		$\Pi_t - D_t$	$\dot{D}_t$	$p_t I_t$
Change in Net worth	$\dot{X}_t^f = \Pi_t - D_t + (\dot{p}_t - \delta p_t) K_t$		$\dot{X}_t^b = \Pi_t^b$	$\dot{X}_t$

**Table:** Balance sheet, transactions, and flow of funds for a three-sector economy.

## ■ Macroeconomic model for climate change

*Productivity*

- The Business as usual Scenario

$$\frac{\dot{a}}{a} = \alpha$$

- The Burke et al.(2015) Scenario

$$\frac{\dot{a}}{a} = \alpha_1 T_\alpha + \alpha_2 T_\alpha^2$$

- The Kaldor-Verdoorn (2002) Scenario

$$\frac{\dot{a}}{a} = \alpha + \eta g$$

- The Gordon (2014) Scenario - productivity growth is 1,3%  
*développeur d'avenirs durables*

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## ■ Climate Module

*CO<sub>2</sub> Emissions*

Global emissions are the sum of industrial and land-use emissions

$$E := E_{ind} + E_{land},$$

where industrial emissions depend on output,

$$E_{ind} := Y\sigma(1 - n),$$

with,

$$\frac{\dot{\sigma}}{\sigma} = -g_\sigma$$

$$\frac{\dot{g}_\sigma}{g_\sigma} = \delta_{g_\sigma} \text{ with } \delta_{g_{sigma}} < 0$$

and the land-use emissions,

$$\frac{\dot{E}_{land}}{E_{land}} = \delta_E \text{ with } \delta_E < 0$$

## ■ Climate Module

### *CO<sub>2</sub> Accumulation*

The CO<sub>2</sub> evolves according to a three-layer model, the atmosphere (AT), the upper ocean (UP) and the lower ocean (LO),

$$\begin{pmatrix} \dot{CO_2}_{AT} \\ \dot{CO_2}_{UP} \\ \dot{CO_2}_{LO} \end{pmatrix} = \begin{pmatrix} E \\ 0 \\ 0 \end{pmatrix} + \begin{pmatrix} -\phi_{12} & \phi_{12} \frac{C_{AT_{eq}}}{C_{UP_{eq}}} & 0 \\ \phi_{12} & -\phi_{12} \frac{C_{AT_{eq}}}{C_{UP_{eq}}} - \phi_{23} & \phi_{23} \frac{C_{UP_{eq}}}{C_{LO_{eq}}} \\ 0 & \phi_{23} & -\phi_{23} \frac{C_{UP_{eq}}}{C_{LO_{eq}}} \end{pmatrix} \begin{pmatrix} CO_2^{AT} \\ CO_2^{UP} \\ CO_2^{LO} \end{pmatrix}.$$

## ■ Climate Module

### Radiative Forcing

Radiative forcing is the sum of the radiative forcing due to CO<sub>2</sub> and other gases,

$$F := F_{ind} + F_{exo},$$

with,

$$F_{ind}(t) = \frac{F_{2\times CO_2}}{\log(2)} \log \left( \frac{C_{CO_2(t)}}{C_{CO_2(t_0)}} \right),$$

$$\dot{F}_{exo} = \delta_{F_{exo}} F_{exo} \left( 1 - \frac{F_{exo}}{F_{exo}^{max}} \right).$$

## ■ Climate Module

### *Temperature Increase*

The temperature dynamics is a two-layer model, with  $T$  being the mean atmospheric temperature deviation with respect to its value in 1900 and  $T_0$  represents the deep-ocean temperature deviation.

$$\begin{aligned} C\dot{T} &= F - (RF)T - \gamma^*(T - T_0) \\ C_0\dot{T}_0 &= \gamma^*(T - T_0) \end{aligned}$$

## ■ Climate Module

### *Damage Function (1/2)*

- The Nordhaus's Damage function (2013),

$$\mathbf{D} = 1 - \frac{1}{1 + \pi_1 T + \pi_2 T^2}$$

- The Weitzman's (2010) and Dietz-Stern's (2015) Damage functions,

$$\mathbf{D} = 1 - \frac{1}{1 + \pi_1 T + \pi_2 T^2 + \pi_3 T^{6.754}}$$

- In Weitzman (2010),  $\pi_3$  is calibrated so that  $\mathbf{D} = 50\%$  whenever  $T = 6$ .
- In Dietz-Stern (2015),  $\pi_3$  is calibrated so that  $\mathbf{D} = 50\%$  whenever  $T = 4$ .

## ■ Climate Module

### Damage Function (2/2)

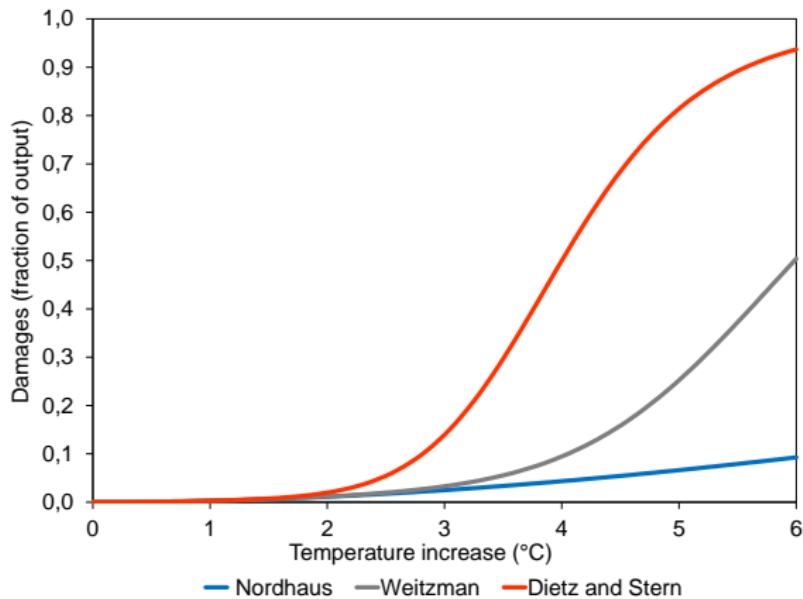


Figure: Comparison of the proposed Damage functions as percentage of output.

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## ■ Public Policy Module

### *Abatement Costs*

The abatement cost

$$G := \theta_1 n^{\theta_2}$$

with  $\theta_1$  and  $\theta_2$  borrowed from Nordhaus (2013).  $n$ , the reduction rate of emissions implied by the abatement cost evolves according to,

$$n = \min \left\{ \left( \frac{p_c}{p_{BS}} \right)^{\frac{1}{\theta_2 - 1}}; 1 \right\}.$$

Prices are exogenously given so that,

$$\frac{\dot{p}_{BS}}{p_{BS}} = \delta_{p_{BS}}, \text{ with } \delta_{p_{BS}} < 0$$

$$\frac{\dot{p}_c}{p_c} = \delta_{p_c}, \text{ with } \delta_{p_c} > 0$$

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## ■ Numerical Simulations

### *Scenarios - Baseline Calibration*

Parameter	Value
$Y_{init}$	64.4565
$N_{init}$	4.5510
$\omega_{init}$	0.5849
$\lambda_{init}$	0.6910
$d_{init}$	1.4393
$p_{init}$	1
$\eta_p$	0.0819
<i>markup</i>	1.610
Monetary illusion	-
$\delta$	0.0625
$\nu$	2.8956
$r$	0.0303
dfi	0.1672
$\alpha$	0.0226

# Numerical Simulations

## The BAU Scenario

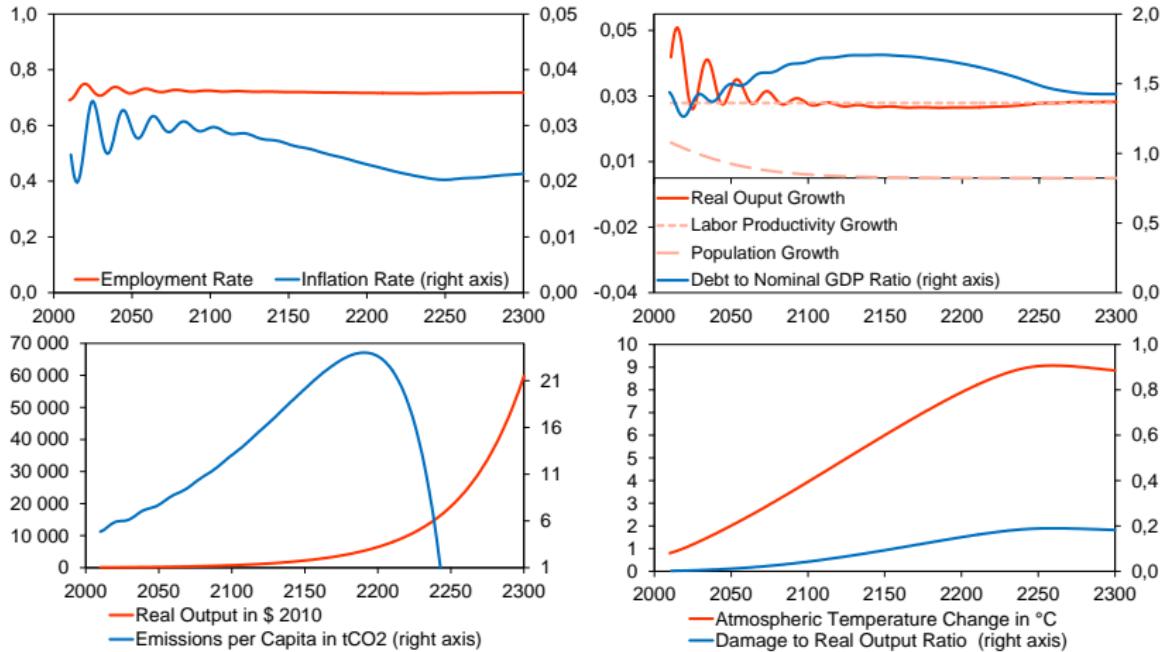
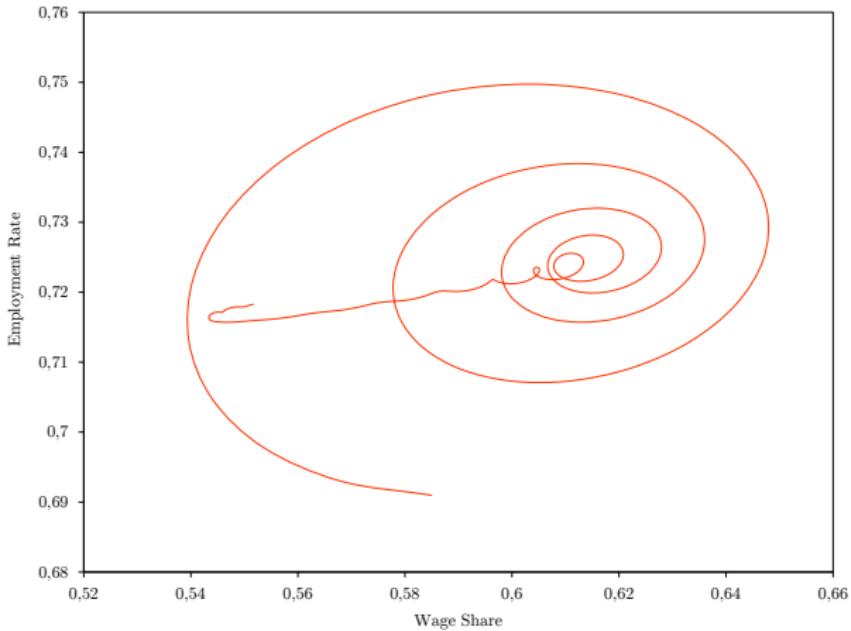


Figure: Trajectories of the main simulation outputs in the BAU case.

# Numerical Simulations

## *The BAU Scenario*



**Figure:** Trajectories of the main simulation outputs in the BAU case.

# Numerical Simulations

## The BAU Scenario

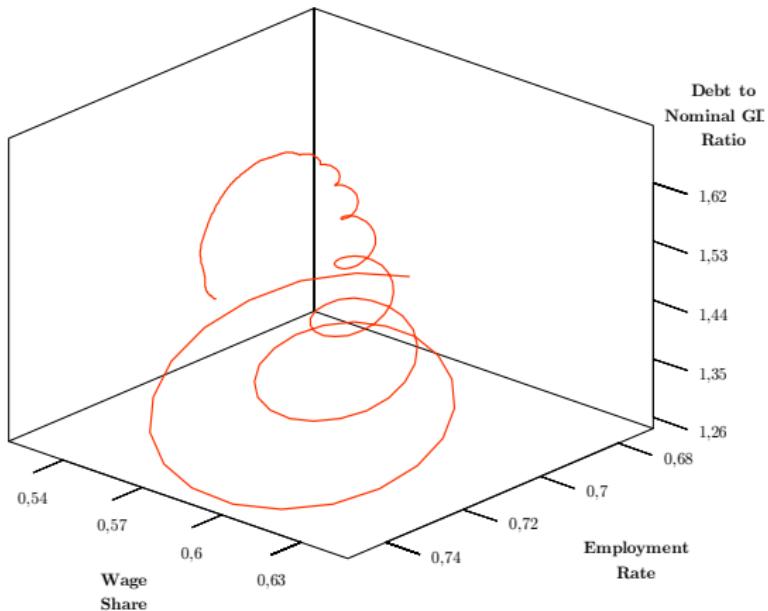


Figure: Trajectories of the main simulation outputs in the BAU case.

## ■ Numerical Simulations

### *The BAU Scenario - Values*

GDP Real Growth 2100 (wrt 2010)	1053%
t CO <sub>2</sub> per capita (2050)	7.72
Temperature change in 2100	+3.94 °C
CO <sub>2</sub> concentration 2100	968.98 ppm

Table: Key values of the world economy by 2100 — the exogenous case.

# Numerical Simulations

## The Kaldor-Verdoorn Scenario

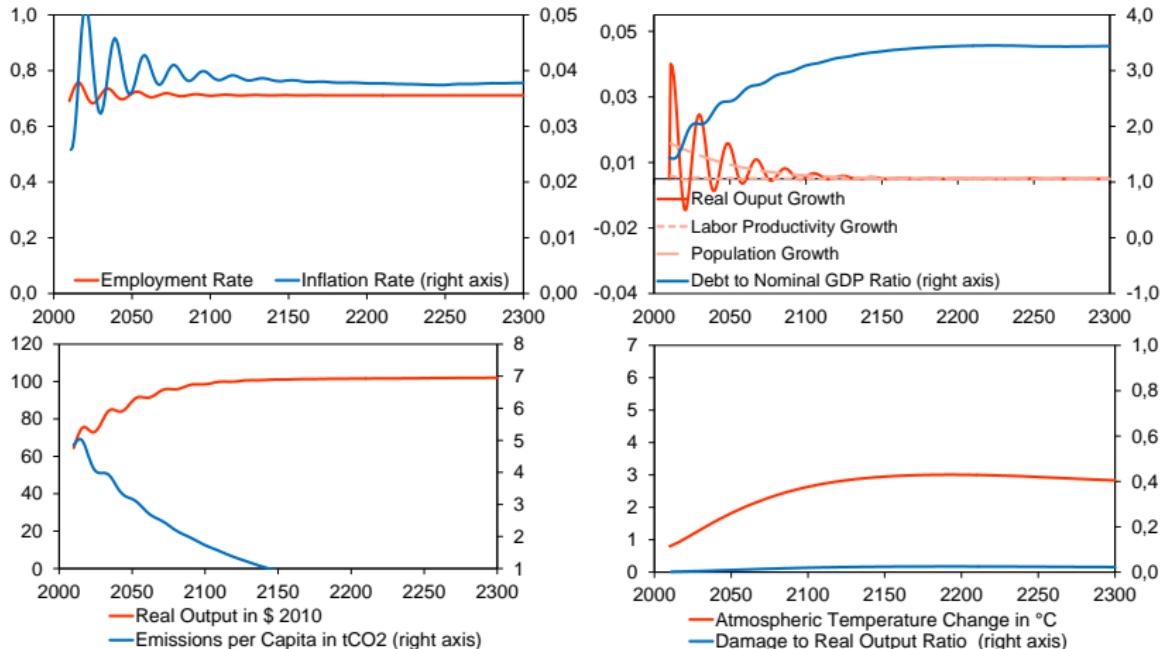


Figure: Trajectories of the main simulation outputs in the Kaldor-Verdoorn case.

## Numerical Simulations

### The Kaldor-Verdoorn Scenario

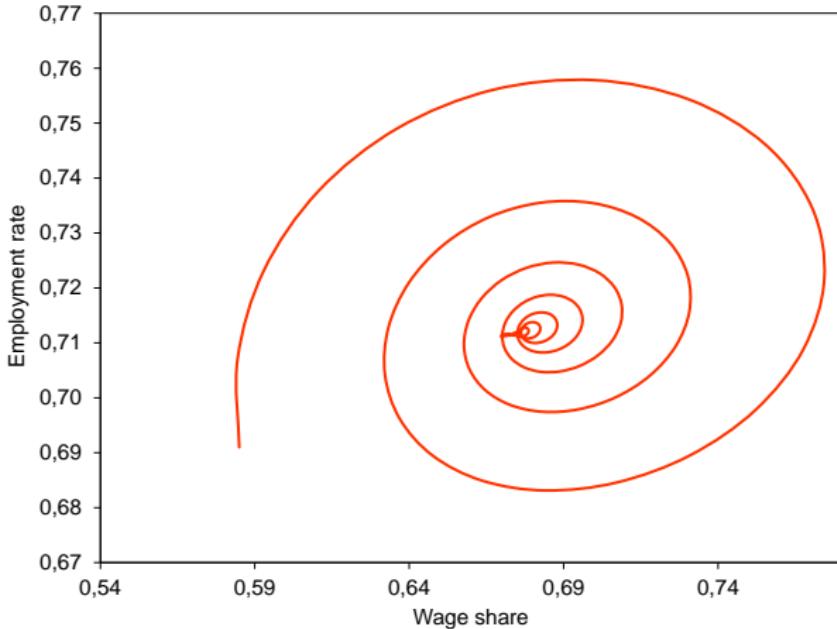


Figure: Trajectories of the main simulation outputs in the Kaldor-Verdoorn case.

## ■ Numerical Simulations

*The Kaldor-Verdoorn Scenario - Values*

GDP Real Growth 2100 (wrt 2010)	53%
t CO <sub>2</sub> per capita (2050)	3.17
Temperature change in 2100	+2.63 °C
CO <sub>2</sub> concentration 2100	521.09 ppm

**Table:** Key values of the world economy by 2100 — the Kaldor-Verdoorn case.

# Numerical Simulations

*The Burke et al. (2015) Scenario*

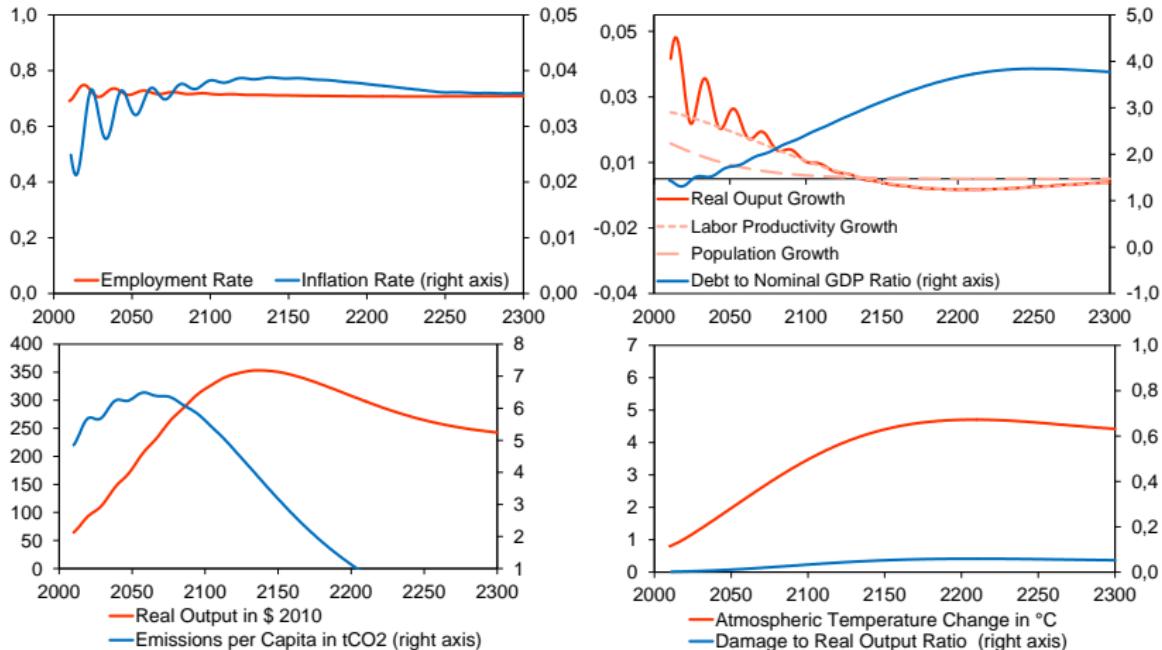


Figure: Trajectories of the main simulation outputs in the Burke et al. (2015) case.

## ■ Numerical Simulations

*The Burke et al. (2015) Scenario*

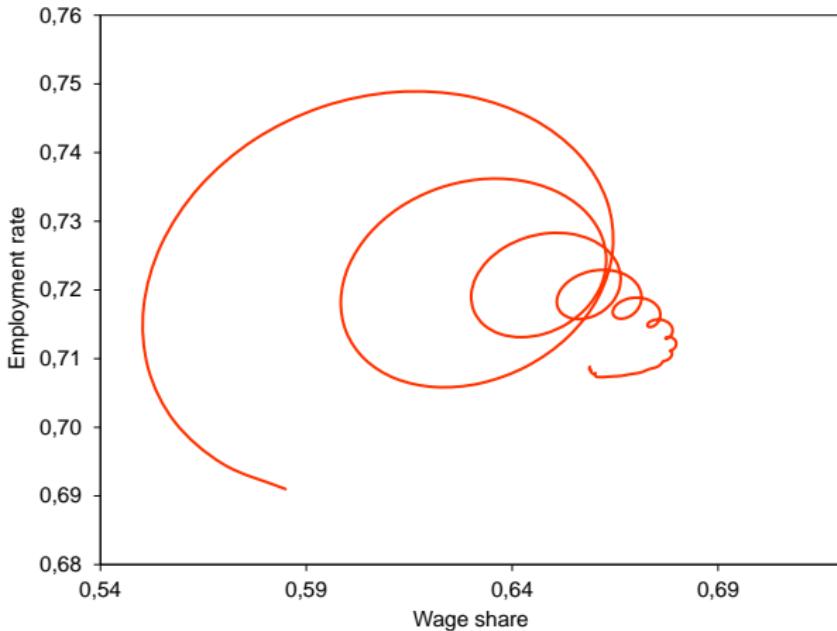


Figure: Trajectories of the main simulation outputs in the Burke et al. (2015) case.

## ■ Numerical Simulations

*The Burke et al. (2015) Scenario - Values*

GDP Real Growth 2100 (wrt 2010)	397%
t CO <sub>2</sub> per capita (2050)	6.29
Temperature change in 2100	+3.48 °C
CO <sub>2</sub> concentration 2100	744.49 ppm

**Table:** Key values of the world economy by 2100 — The Burke et al. (2015) case.

# Numerical Simulations

## The Weitzman Scenario

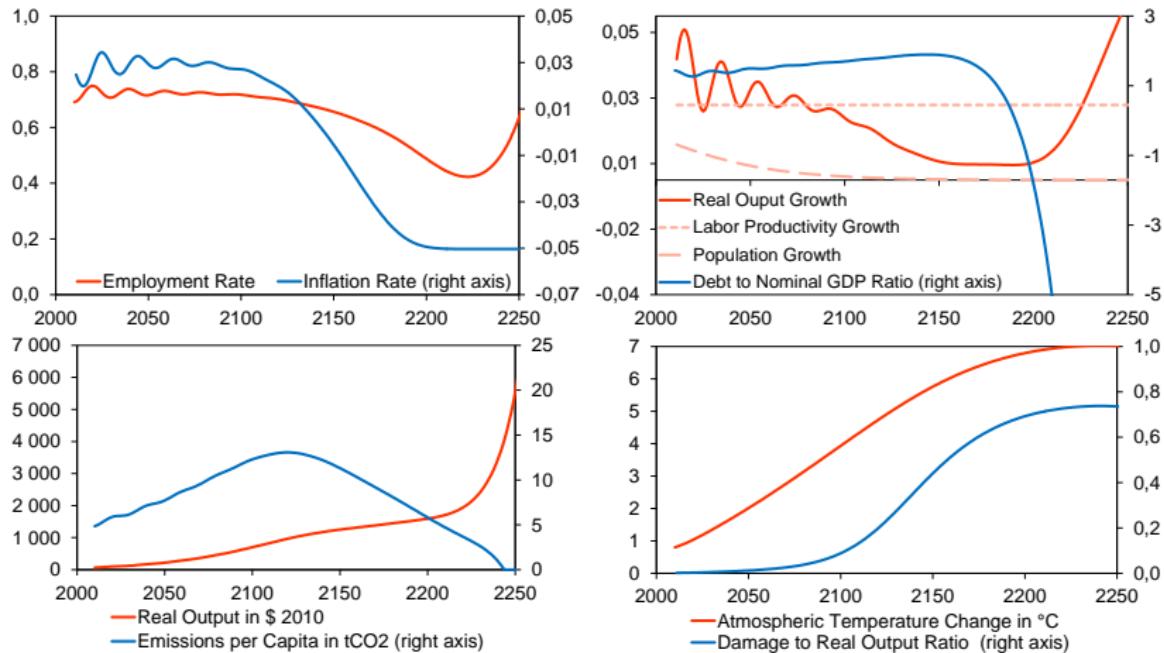


Figure: Trajectories of the main simulation outputs in the Weitzman case.

## Numerical Simulations

### *The Weitzman Scenario*

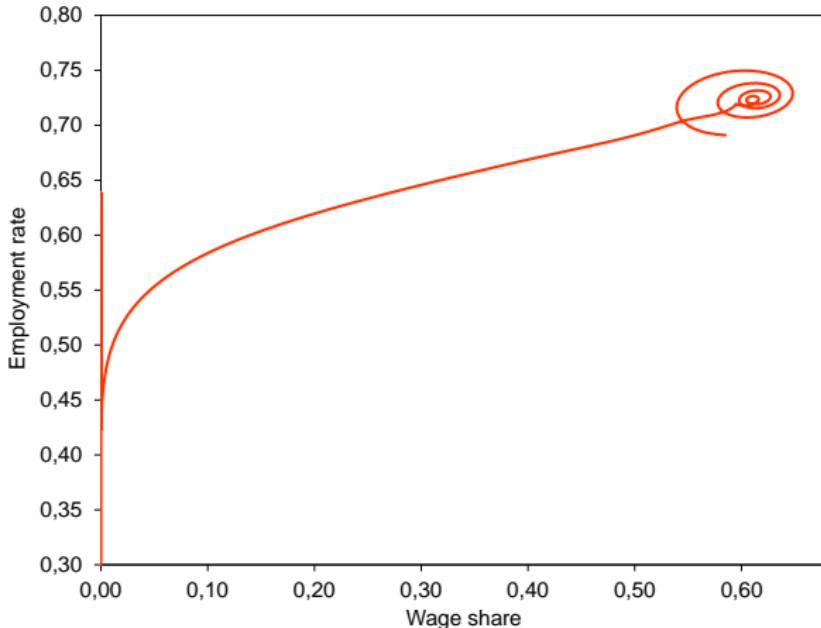


Figure: Trajectories of the main simulation outputs in the Weitzman case.

## ■ Numerical Simulations

### *The Weitzman Scenario - Values*

GDP Real Growth 2100 (wrt 2010)	987%
t CO <sub>2</sub> per capita (2050)	7.72
Temperature change in 2100	+3.93 °C
CO <sub>2</sub> concentration 2100	958.17 ppm

Table: Key values of the world economy by 2100 — the Weitzman case.

# Numerical Simulations

## The Dietz-Stern Scenario

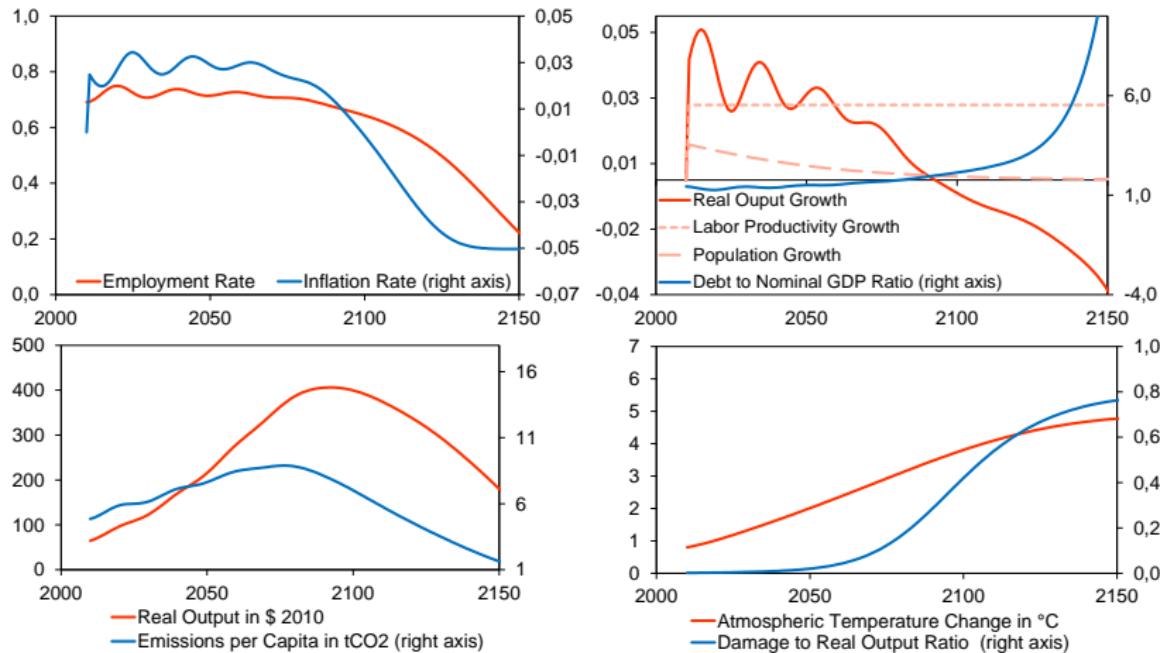


Figure: Trajectories of the main simulation outputs in the Dietz-Stern case.

## Numerical Simulations

### *The Dietz-Stern Scenario*

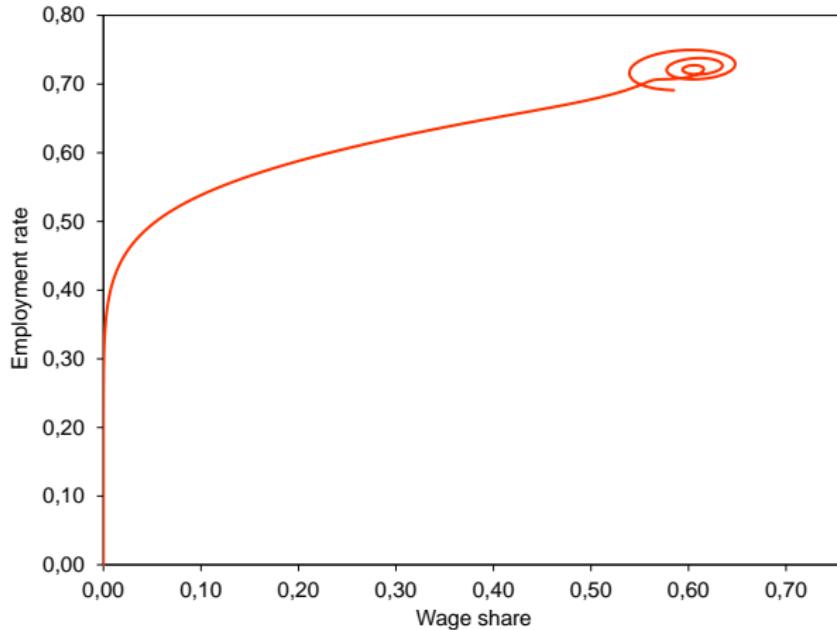


Figure: Trajectories of the main simulation outputs in the Dietz-Stern case.

## ■ Numerical Simulations

### *The Dietz-Stern Scenario - Values*

GDP Real Growth 2100 (wrt 2010)	495%
t CO <sub>2</sub> per capita (2050)	7.72
Temperature change in 2100	+3.84 °C
CO <sub>2</sub> concentration 2100	860.53 ppm

Table: Key values of the world economy by 2100 — the Dietz-Stern case.

# Numerical Simulations

The Combined Burke et al. and Dietz-Stern Scenario

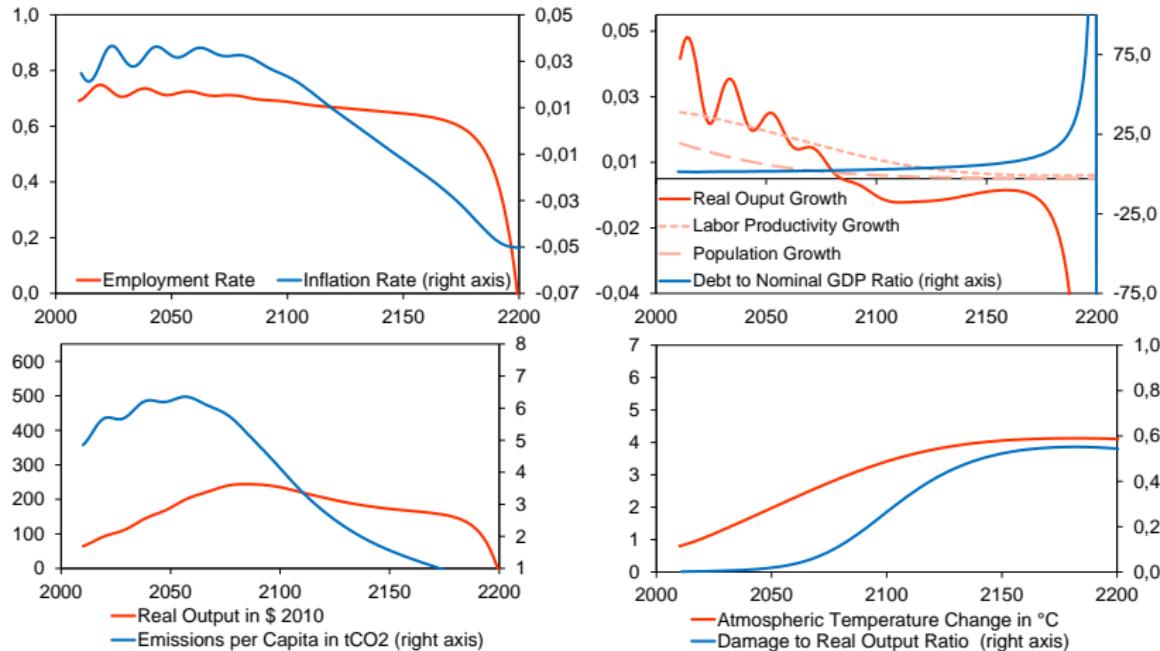


Figure: Trajectories of the main simulation outputs in the Combined Burke et al. and Dietz-Stern case.

## Numerical Simulations

*The Combined Burke et al. and Dietz-Stern Scenario*

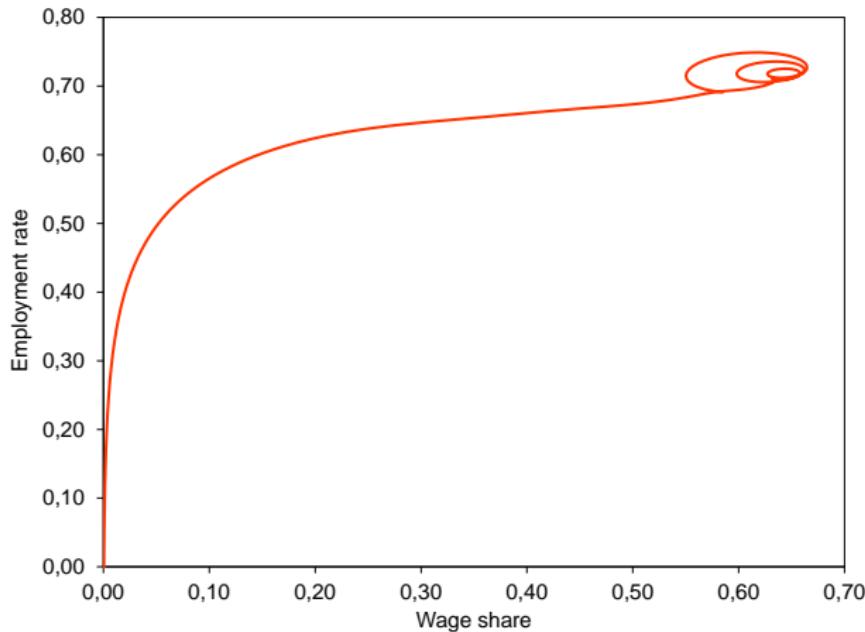


Figure: Phase portrait in the Combined Burke *et al.* and Dietz-Stern case

## ■ Numerical Simulations

*The Combined Burke et al. and Dietz-Stern - Values*

GDP Real Growth 2100 (wrt 2010)	265%
t CO <sub>2</sub> per capita (2050)	6.23
Temperature change in 2100	+3.41 °C
CO <sub>2</sub> concentration 2100	708.98 ppm

**Table:** Key values of the world economy by 2100 — The Combined Burke et al. and Dietz-Stern case.

## Numerical Simulations

The Combined Burke et al. and Dietz-Stern - Demographic

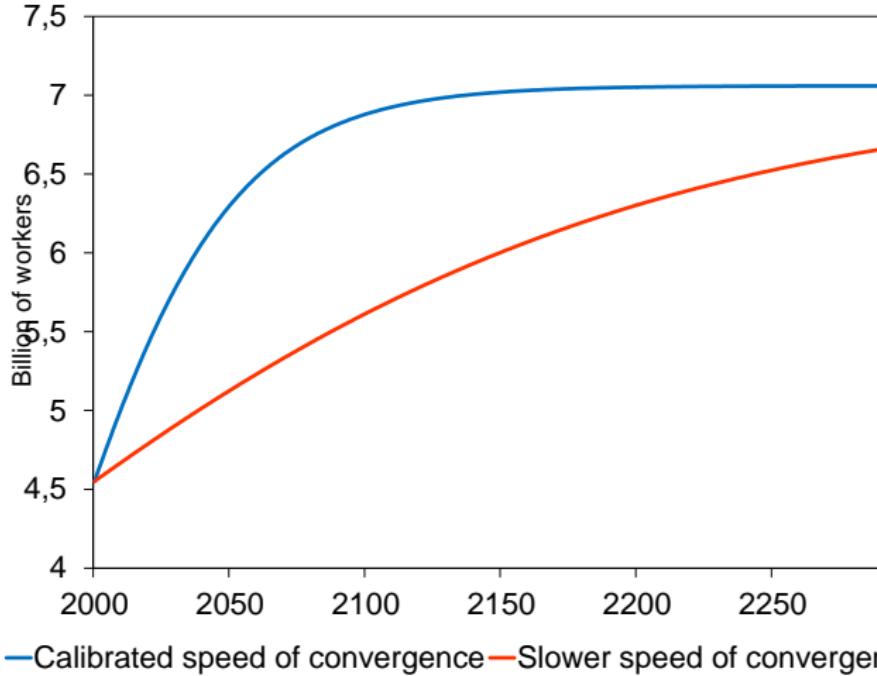


Figure: Trajectories of the main simulation outputs in the Combined Burke et al. and Dietz-Stern - Demographic.

# Numerical Simulations

## The Combined Burke-Dietz Scenario - Demographic

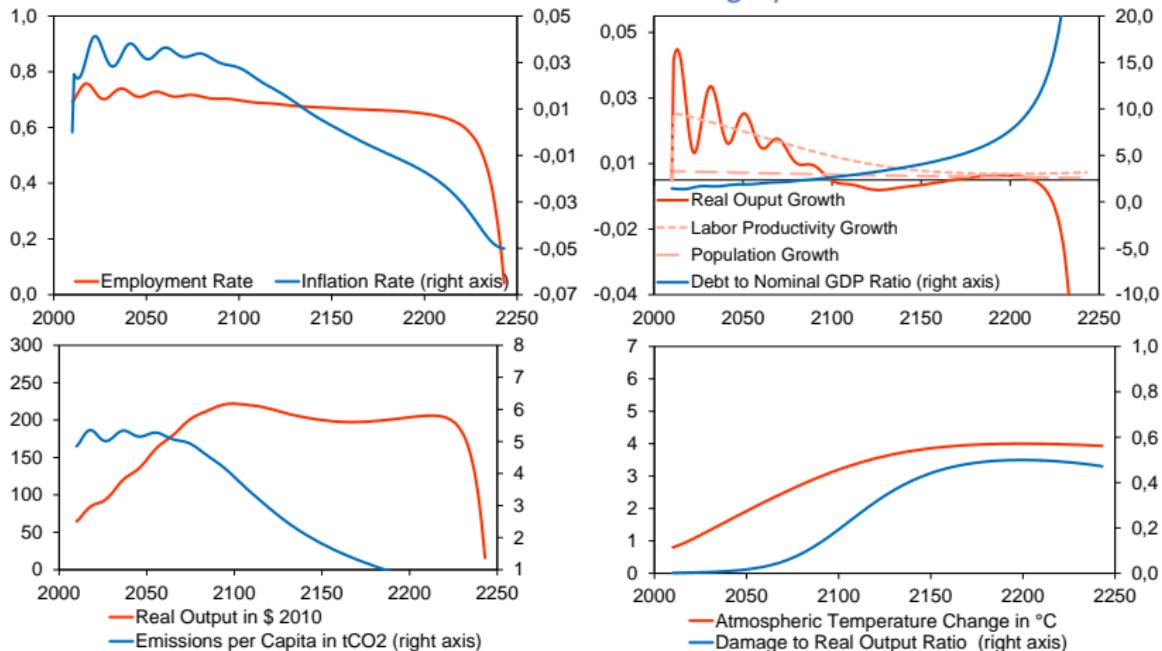


Figure: Trajectories of the main simulation outputs in the Combined Burke et al. and Dietz-Stern - Demographic.

## ■ Numerical Simulations

*The Combined Burke et al. and Dietz-Stern - Demographic - Values*

GDP Real Growth 2100 (wrt 2010)	244%
t CO <sub>2</sub> per capita (2050)	5.21
Temperature change in 2100	+3.20 °C
CO <sub>2</sub> concentration 2100	660.37 ppm

**Table:** Key values of the world economy by 2100 — the Combined Burke et al. and Dietz-Stern - Demographic.

## ■ Numerical Simulations

### *Price of Carbon*

- we find the initial condition in 2010 that the growth rate that match with the 2015 and 2055 values (2005 \$US 12 and 29 t/CO<sub>2</sub> respectively)

# Numerical Simulations

The Combined Burke et al. and Dietz-Stern - Carbon Price

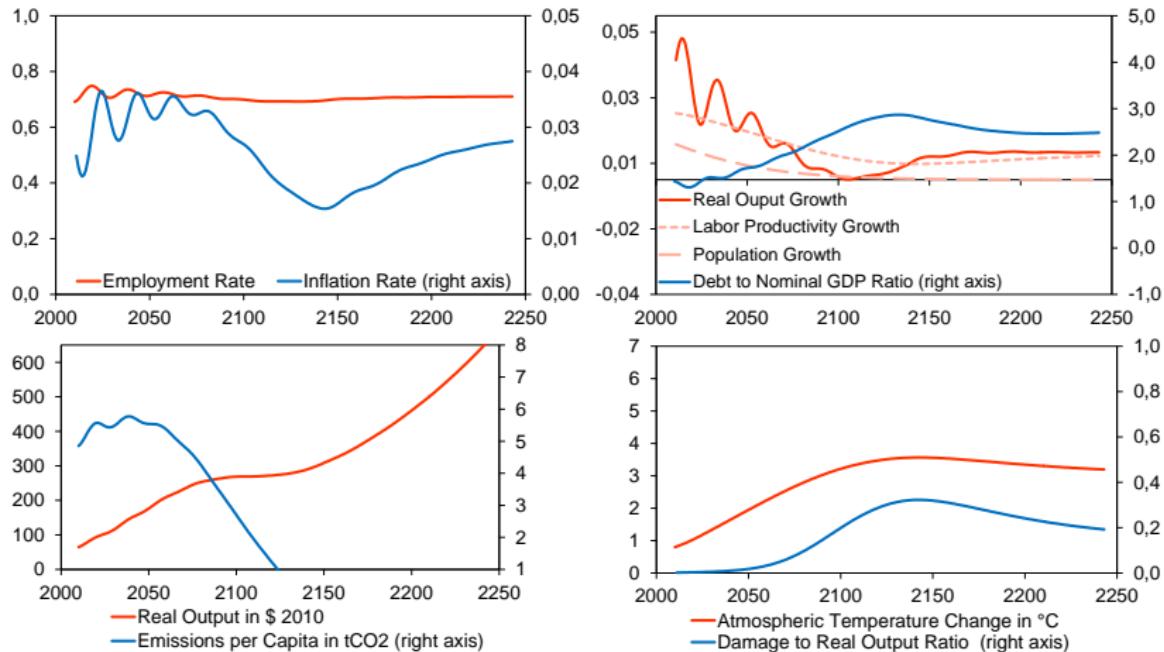


Figure: Trajectories of the main simulation outputs in the Combined Burke et al. and Dietz-Stern - Carbon Price.

## Numerical Simulations

*The Combined Burke et al. and Dietz-Stern - Carbon Price*

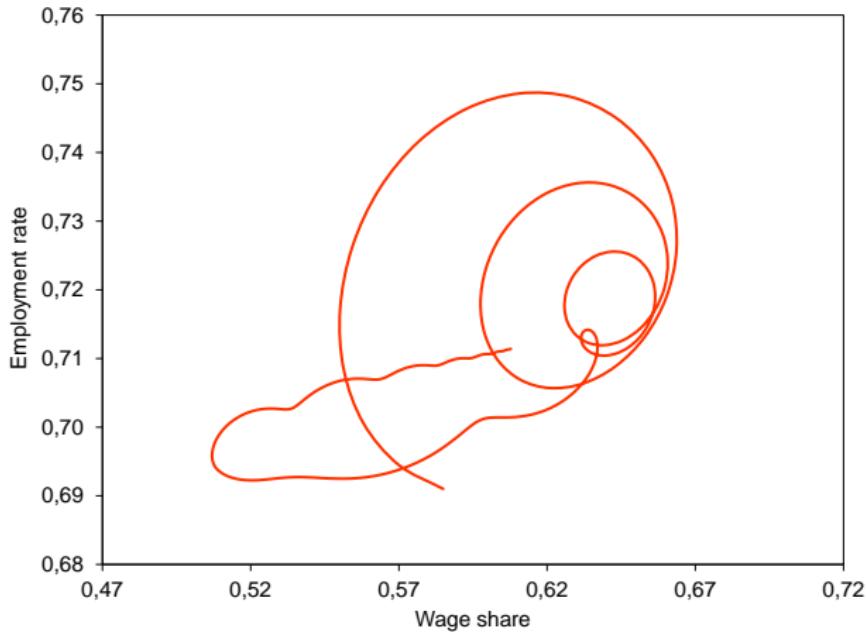


Figure: Trajectories of the main simulation outputs in the Combined Burke et al. and Dietz-Stern - Carbon Price.

## ■ Numerical Simulations

*The Combined Burke et al. and Dietz-Stern - Carbon Price- Values*

GDP Real Growth 2100 (wrt 2010)	3.17%
t CO <sub>2</sub> per capita (2050)	5.54
Temperature change in 2100	+3.22 °C
CO <sub>2</sub> concentration 2100	643.77 ppm

**Table:** Key values of the world economy by 2100 — the Combined Burke *et al.* and Dietz-Stern- Carbon Price.

# Numerical Simulations

The Combined Burke et al. and Dietz-Stern - Carbon Price - Sensitivity of

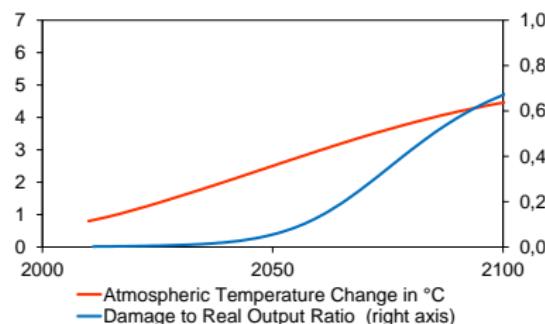
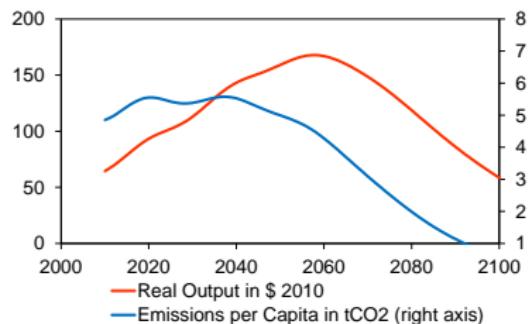
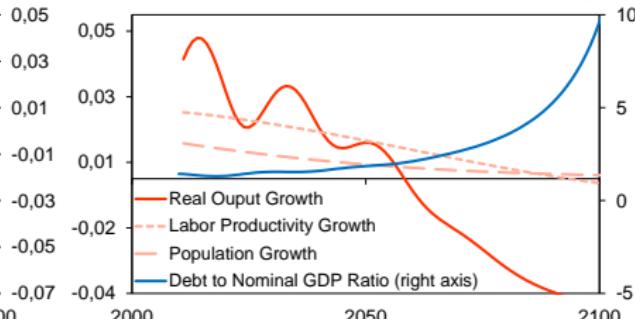
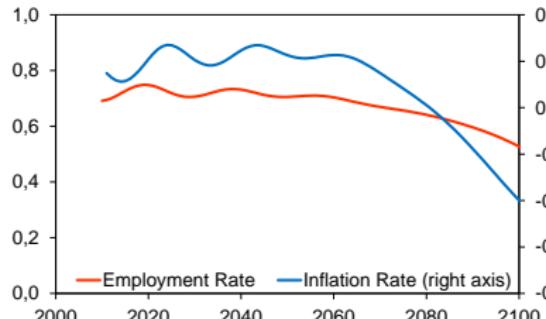


Figure: Trajectories of the main simulation outputs in the Combined Burke-Dietz Scenario - Carbon Price case.

## ■ Numerical Simulations

*The Combined Burke et al. and Dietz-Stern - Carbon Price- Values*

GDP Real Growth 2100 (wrt 2010)	-9.1%
t CO <sub>2</sub> per capita (2050)	5.00
Temperature change in 2100	+4.4552°C
CO <sub>2</sub> concentration 2100	549.78 ppm

**Table:** Key values of the world economy by 2100 — the Combined Burke *et al.* and Dietz-Stern - Carbon Price.

## ■ Numerical Simulations

### *Price of Carbon 2*

- we find the initial condition in 2010 that the growth rate that match with the 2015 and 2055 values (2005 \$US 74 and 306 t/CO<sub>2</sub> respectively)

# Numerical Simulations

The Combined Burke et al. and Dietz-Stern - Carbon Price 2 - Sensitivity

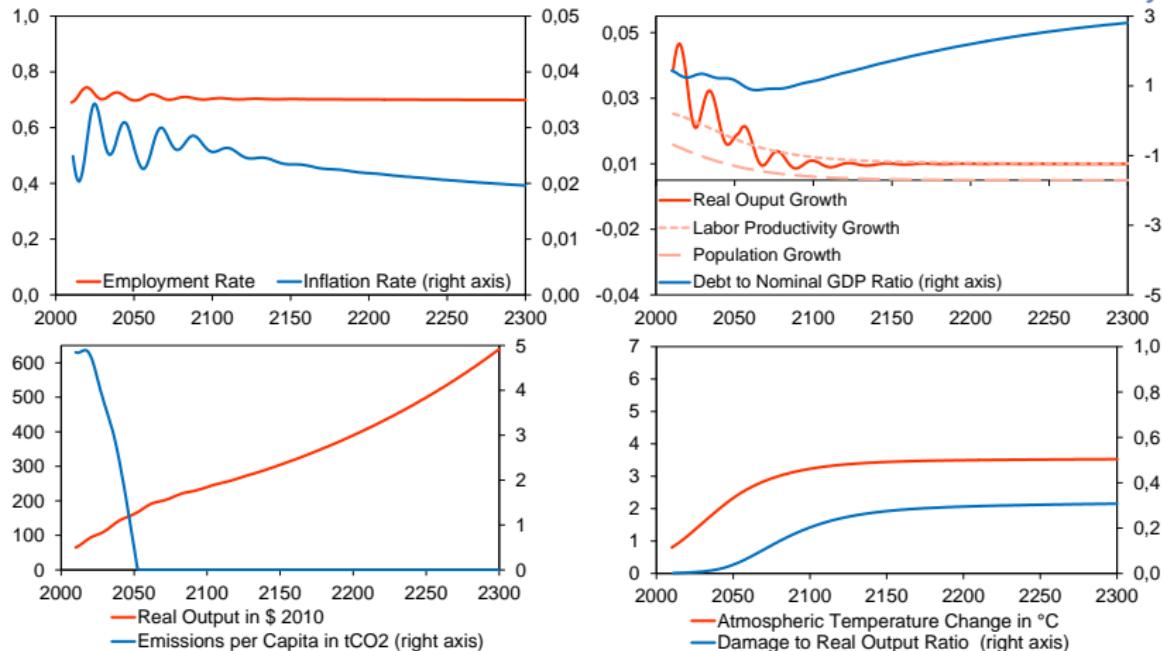


Figure: Trajectories of the main simulation outputs in the Combined Burke et al. and Dietz-Stern - Carbon Price 2 - Sensitivity of 6 case.

## ■ Numerical Simulations

*The Combined Burke et al. and Dietz-Stern - Carbon Price- Values*

GDP Real Growth 2100 (wrt 2010)	272%
t CO <sub>2</sub> per capita (2050)	0.49
Temperature change in 2100	+3.2293°C
CO <sub>2</sub> concentration 2100	397.98 ppm

**Table:** Key values of the world economy by 2100 — the Combined Burke *et al.* and Dietz-Stern - Carbon Price.

## ■ Numerical Simulations

### *Objective 1.5*

- According to the 2015 climate meeting, held in Paris, the universal agreement's main goal is to stay, in this century, within the + 2 C of temperature anomaly and to drive efforts to limit even further to + 1.5C above pre-industrial levels.

## ■ Numerical Simulations

*Objective + 1.5° C*

	Sensitivity of 1.5		Sensitivity of 2.9	
	Init price of 15	Init price of 80	Init price of 15	Init price of 80
Price in 2015	18.58	86.27	65.50	144.32
Price in 2020	23.00	93.04	286.02	260.35
Price in 2050	82.93	146.35	xxx	xxx

**Table:** Price in order to prevent the temperature anomaly to reach the + 1.5° ceiling in 2100, prices are in 2005 US\$/t CO<sub>2</sub>.

# ■ Outlines

- 1 Introduction
- 2 The Keen (1995) Model
- 3 Macroeconomic model for climate change
- 4 Climate Module
- 5 Public Policy Module
- 6 Numerical Simulations
- 7 Further Work

## ■ Further Work

*Further work*

- To model non-renewable energy, natural resource scarcity.
- To introduce the public sector.
- To refine the statistical framework.
- To distinguish the agricultural from the industrial production.
- To precise the determination of the damage functions.



Thank you for your attention.

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développeur d'avenirs durables